



How can ab initio simulations help the PV industry ?

Julien Vidal

EDF R&D

In collaboration with A. Zakutayev, S. Lany, D. Ginley (NREL), F. DiSalvo (Cornell), R. Haight (IBM Yorktown), S. Delbos (IRDEP)



dépasser les frontières



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Plan

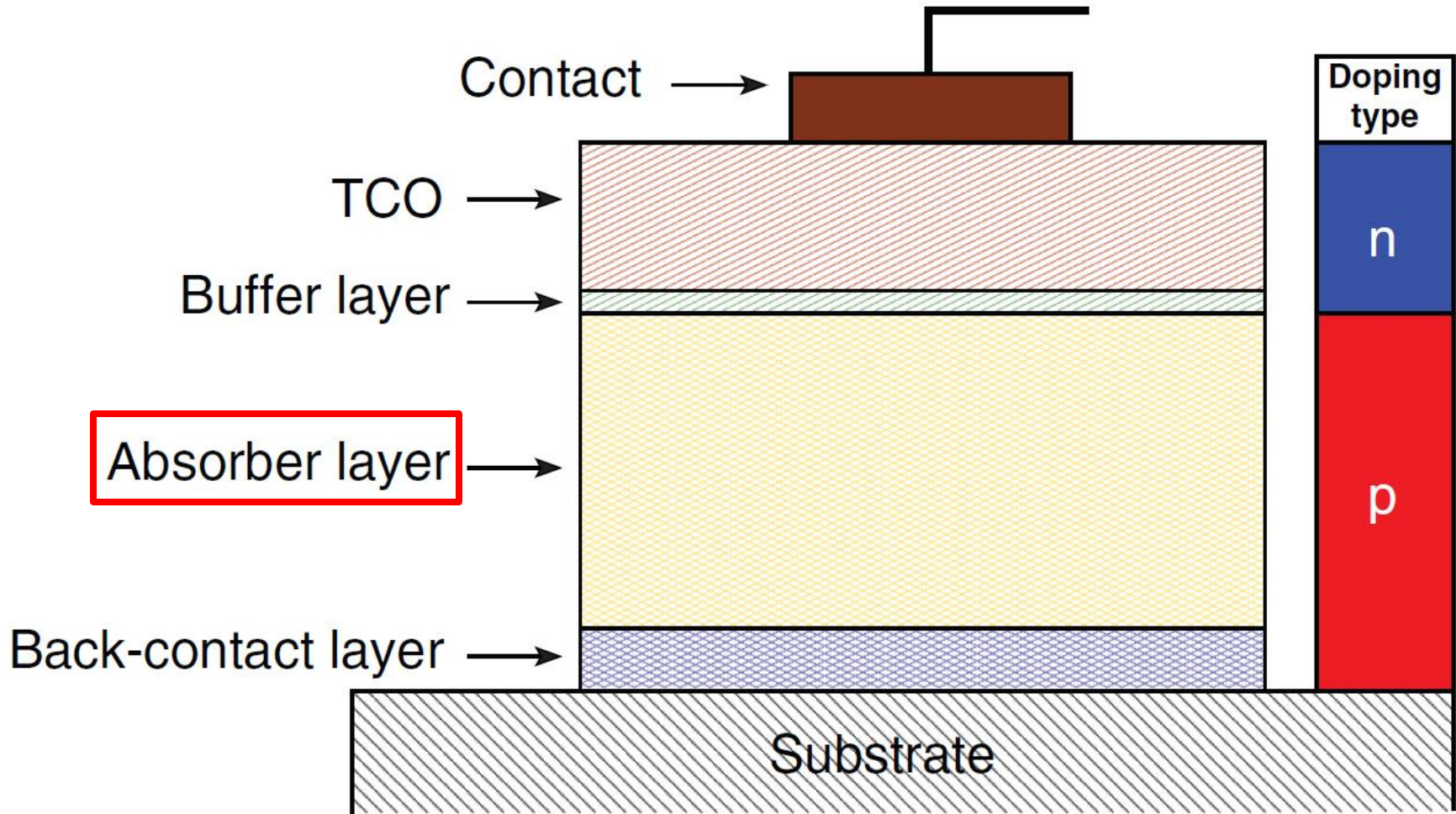
- Thin film solar cells
- Pros and cons of discovery of new materials, an industrial view
- Project Cu-N: new materials
- Project SnS: a rediscovered material
- Project CZTS: a promising material ?
- Conclusion and perspectives



1

THIN FILM SOLAR CELLS

Design of the solar cells



**What is the most critical property
for an absorber material ?**

What is the most critical property for an absorber material ?

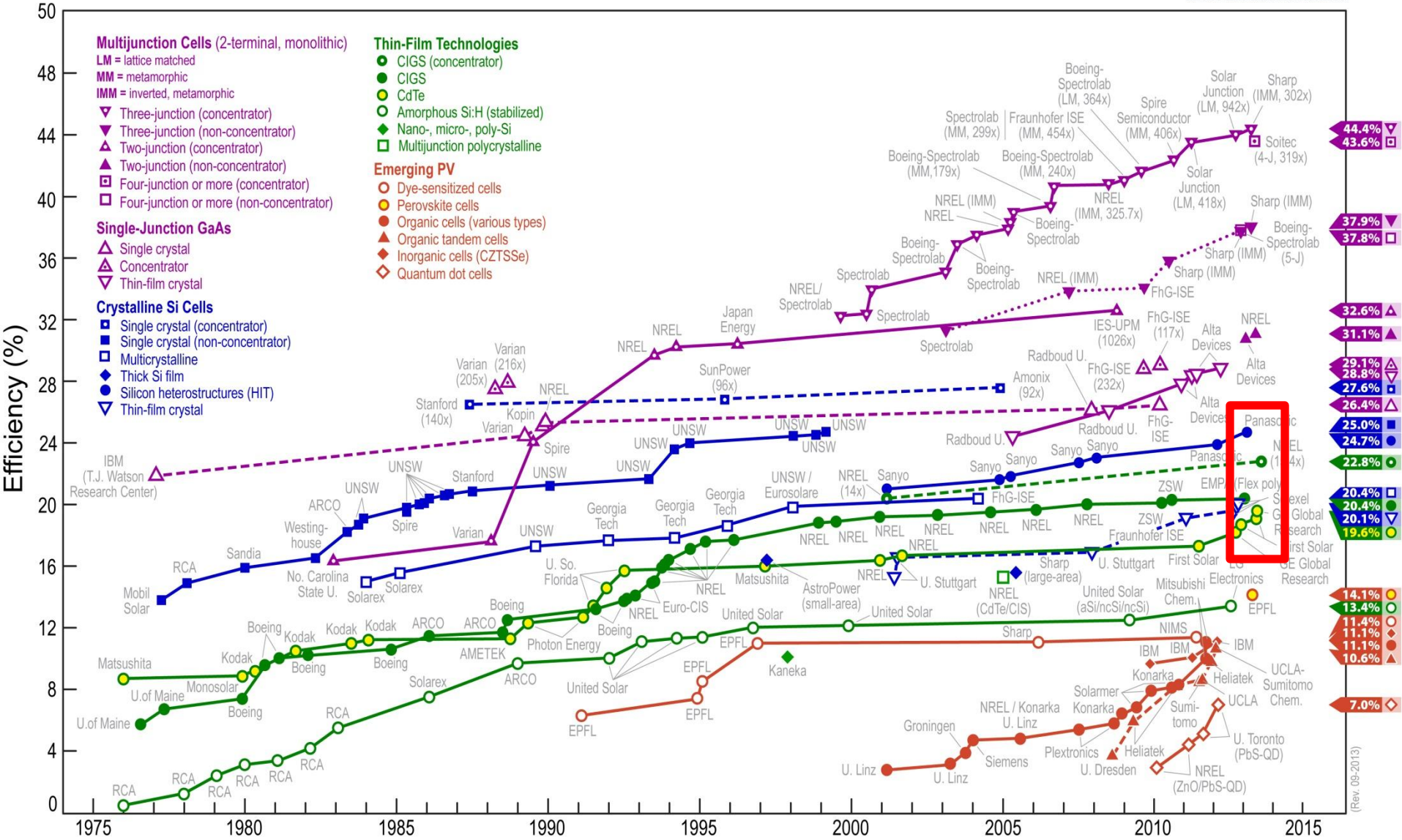
Counterexample: silicon

The most important quantity for the absorber is **carrier lifetime (in Si millisecond)**

Other important quantities: *moderate p-type doping, low minority carrier effective mass, stability under operating conditions, good light absorbing capability.*

Absorbing layer materials

Best Research-Cell Efficiencies





2

PROS AND CONS OF DISCOVERY OF NEW MATERIALS

Pros: commonly publicized motivations

• Socio-economical interest in finding *new materials with desired properties*:

- Indium/Tellurium is rare/expensive preventing the large deployment of CIGS and CdTe-based solar modules.
- Good for the economy !!!!! Lower price for PV modules
- **Consequences**: new PV thin film absorbers such as SnS, CZTS, Fe₂S

• New properties and potentially new physics → new materials:

- Recent discovery of topological states at the surface of HgTe and Bi₂Se₃
- **Consequences**: lots of **theoretically predicted** new topological insulators , few of them actually **realized experimentally**.

Kesong Yang et al., Nature materials, **11**,614, (2012)

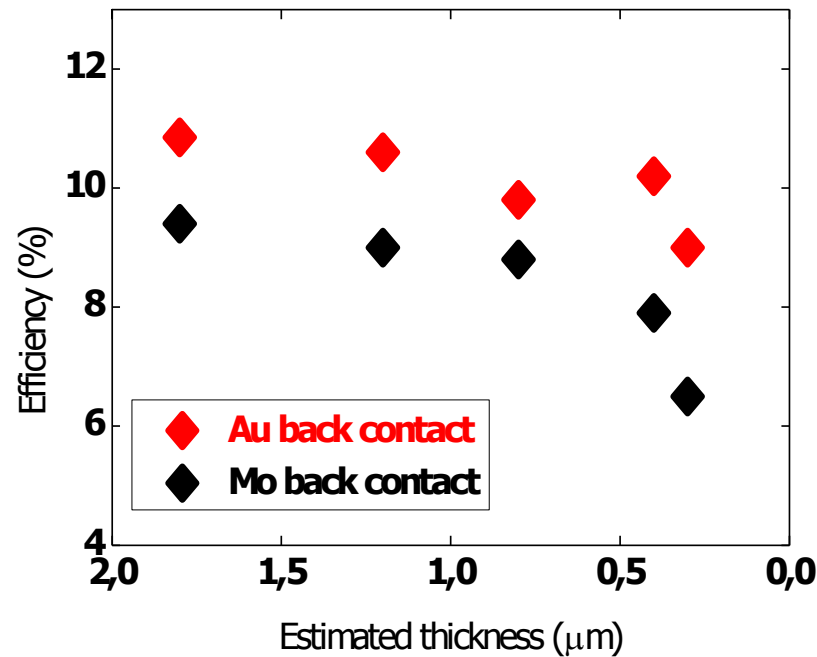
Lot of research initiatives to develop the search for new materials but is it really necessary ?



Cons: not so publicized critics

- **New design could overcome shortage of elements**

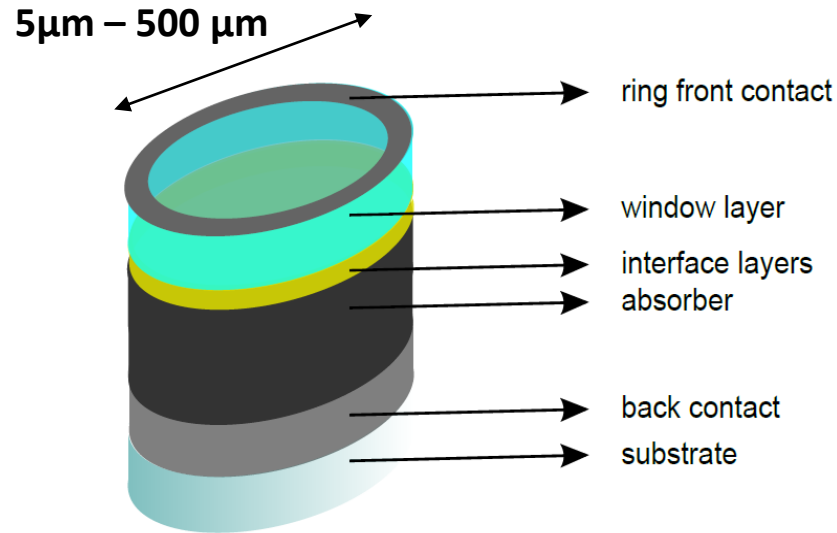
- **Ultra thin CIGS solar cell** → improved light management , new back contact → new materials !!!



Z. Jehl Li Kao et al., Progress in Photovoltaics, 20, 582, 2012

Cons: not so publicized critics

- **New design could overcome shortage of elements**
 - **Micro solar cell under concentration → 0D system**



No concentration+regular thin film: 16% !!!

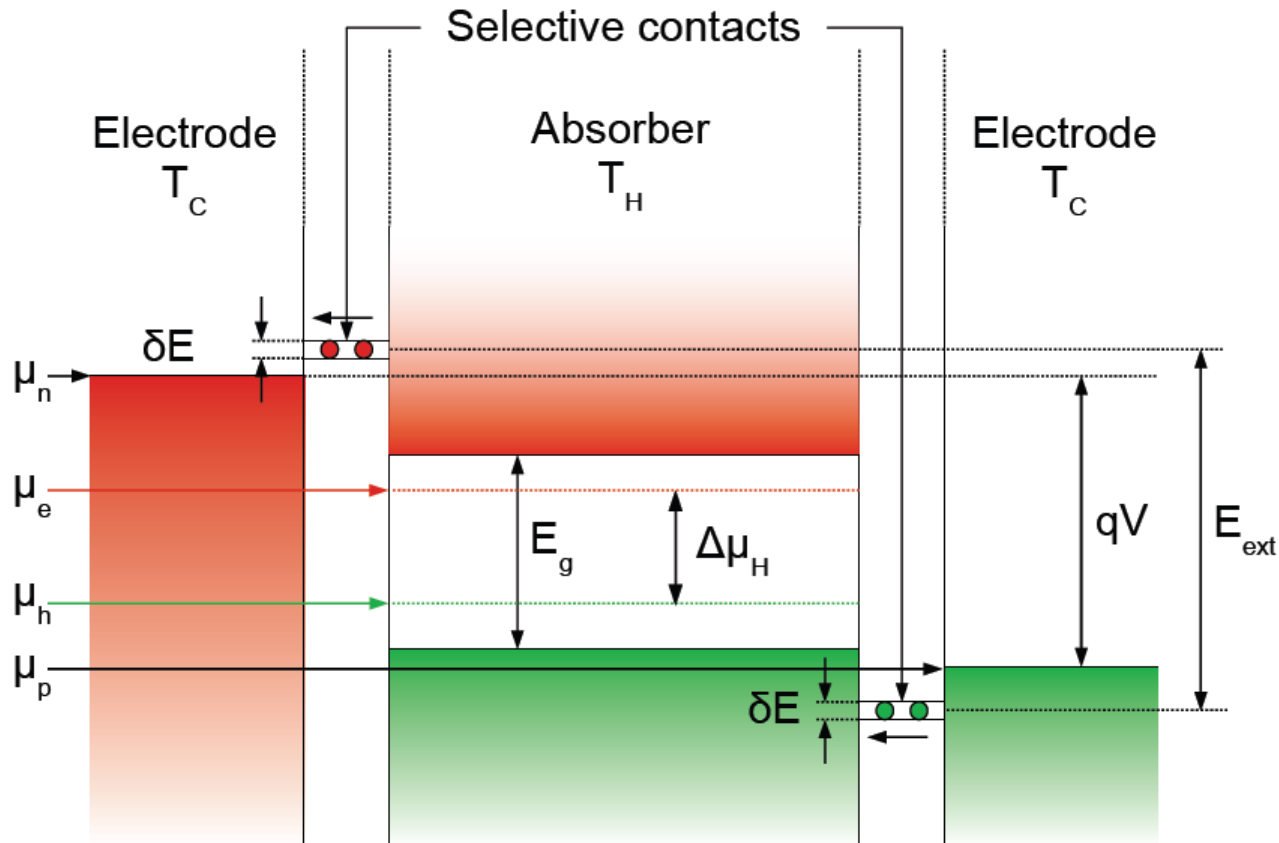
475 x concentration+micro cell: 21.3 % !!!

M. Paire *et al.*, Journal of Renewable Sustainable Energy, 5, 011202 (2013)

M. Paire *et al.*, Energy and Environmental Science, 4, 12, 4972 (2012)

Device design vs desired properties

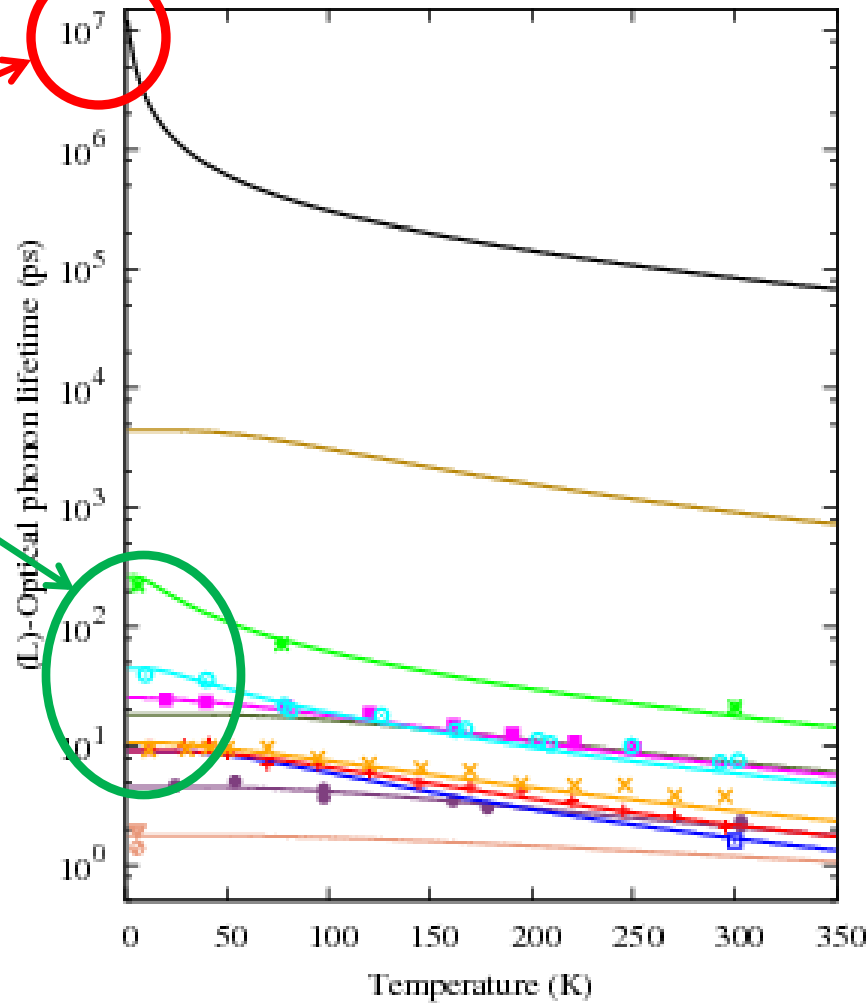
New design: Hot Carrier Solar cells



Desired properties for the absorber: long lifetime of LO phonons

Search for the optimal absorber in HCSC

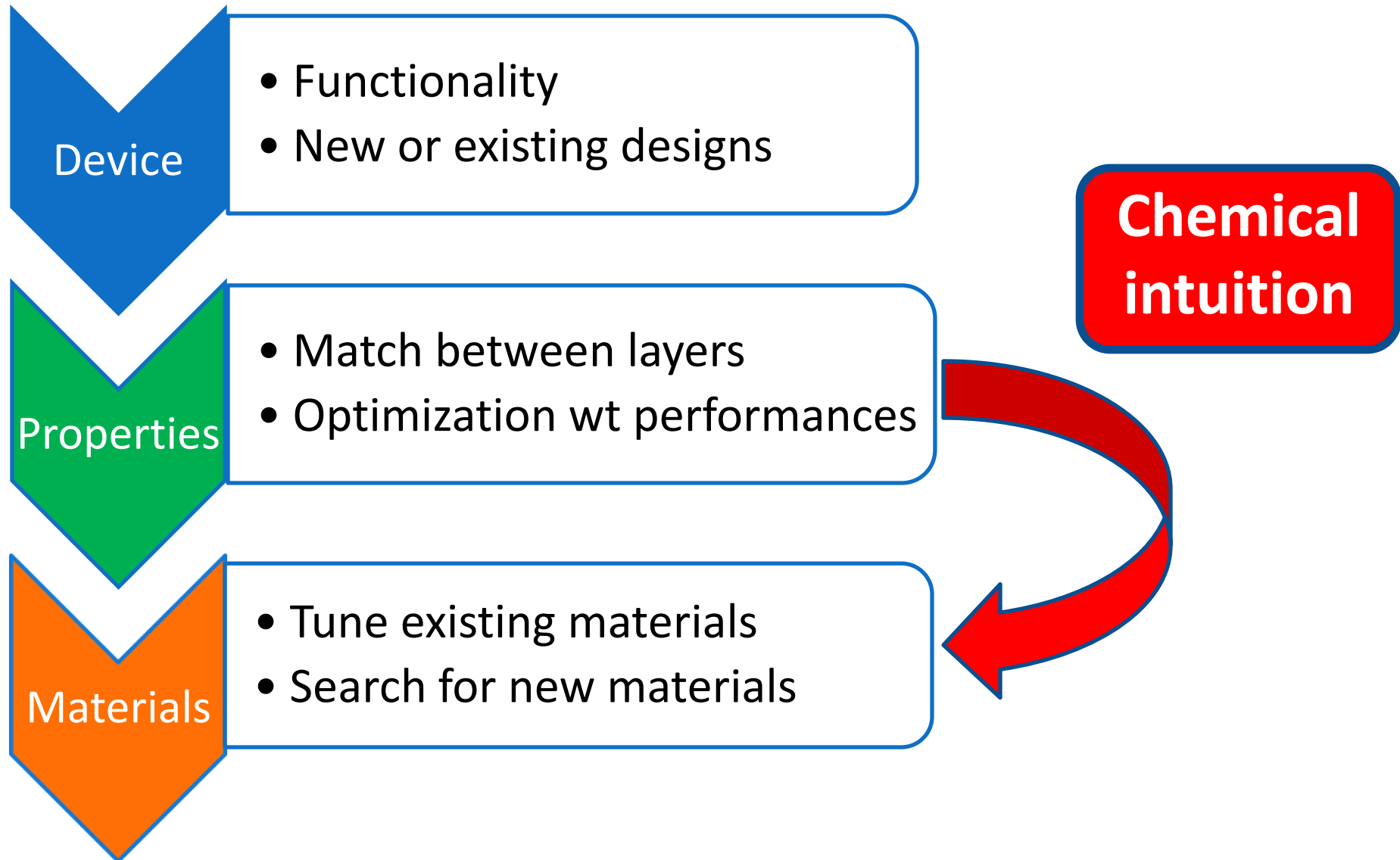
6 orders of magnitude higher than III-V



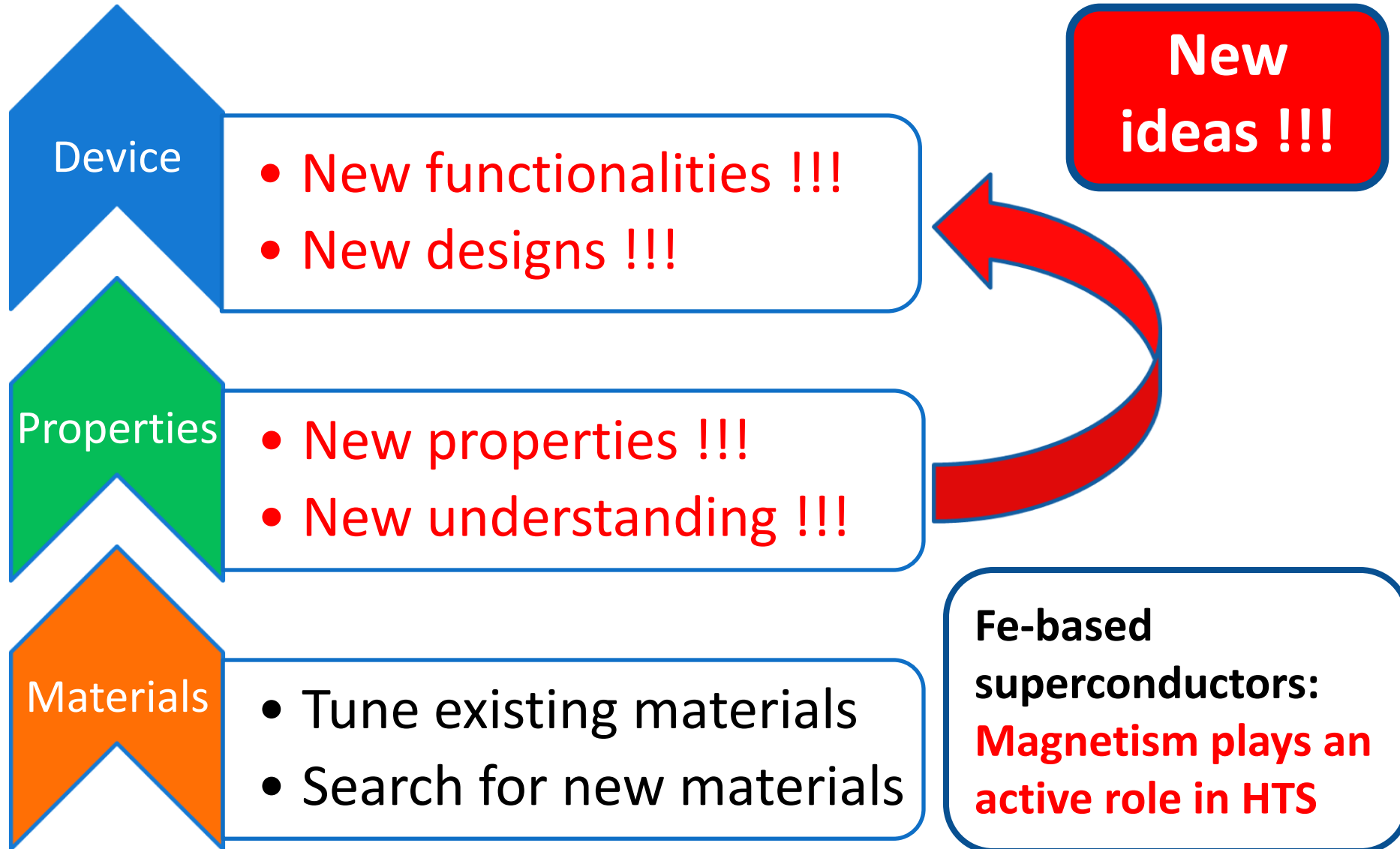
Courtesy of Hugo Levard,
EDF R&D



Current flow chart: top-down



What about bottom up ?





3

CU-N PROJECT

Design and Physical intuitions

- **Design chosen: thin film solar cells**

- p-type doping: 10^{16} - 10^{17} cm⁻³ with no recombination centers.
- High optical absorption in the visible range.
- Good collection properties *i.e.* effective mass

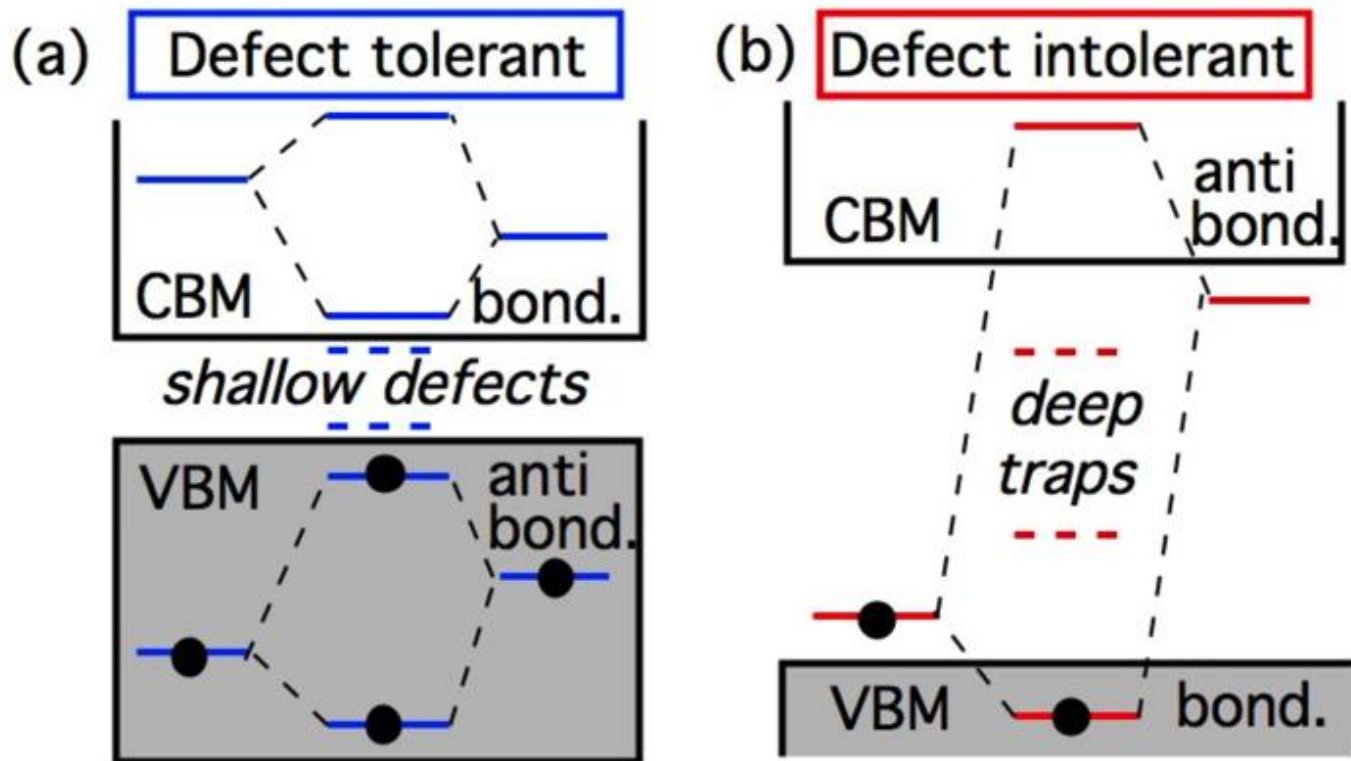
- **Physical intuition**

- Defect immunity and p-doping of CIGS stems from structure of the valence.

Design and Physical intuitions

- **Physical intuition**

- Defect immunity and p-doping of CIGS stems from **structure of the valence**.



Raebiger et al., PRB, 76 , 045209, (2007)

Zakutayev et al., submitted (2013)

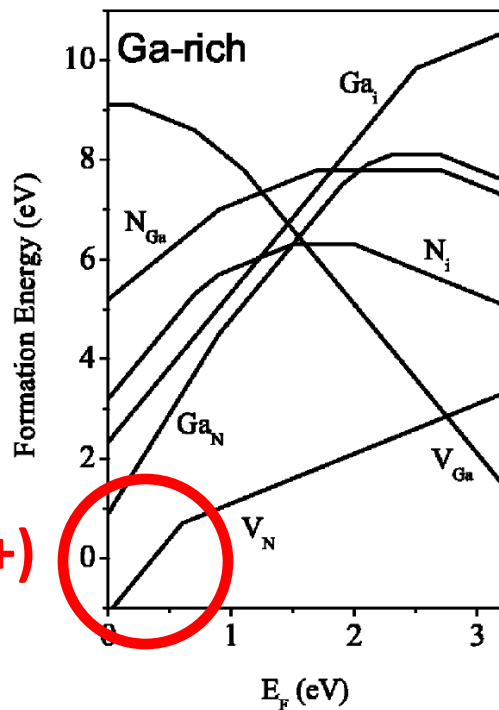
Tuning the Cu-X bonding

• How to tune Cu-X valence width ?

- Match the energy of **p-orbital of X** to the the energy of **d-orbital of Cu**
- Best match: **Cu-N**

• Nitrides and PV ?

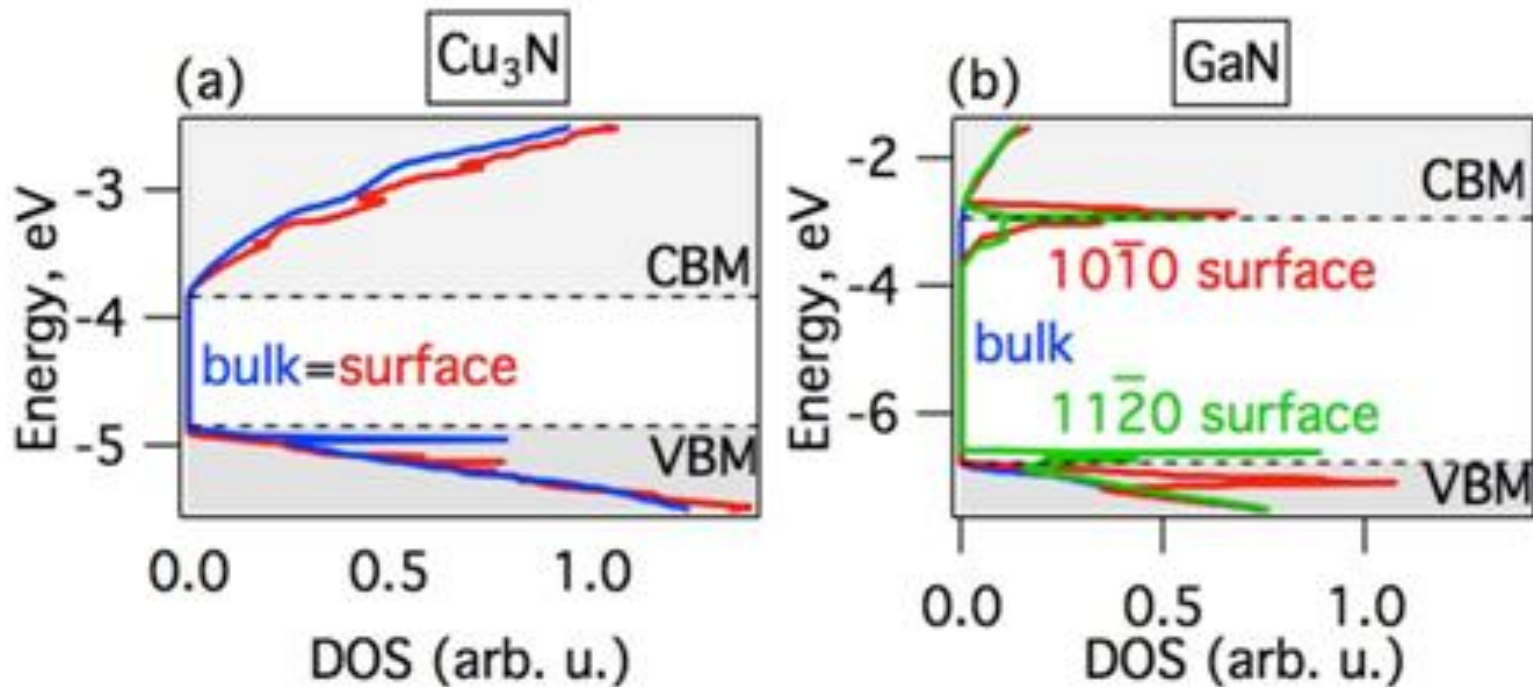
- Serious game player in high efficiency multijunction solar cell
- With respect to CIGS thin film designs ??



- Binary Cu-N \rightarrow **Cu_3N $\Delta H_f > 0$ unstable**
- Low formation energy of $V_N \rightarrow$ **n-type**
- Incorporation of O as $O_N \rightarrow$ **n-type**
- Weird crystal structures \rightarrow **???**
- GaN 3.4 eV to InN 0.7 eV \rightarrow **tunable gap**

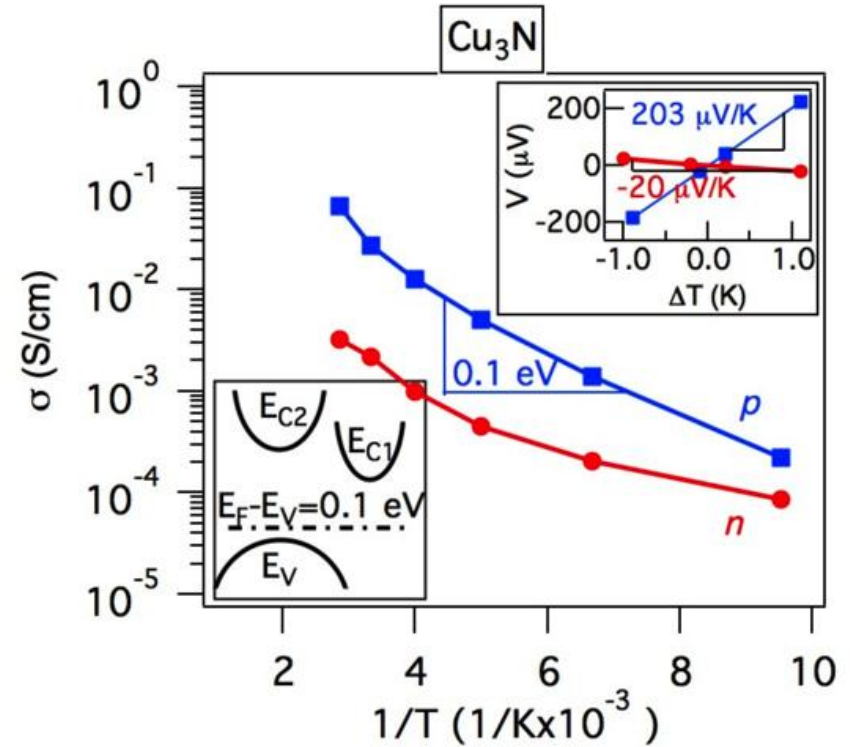
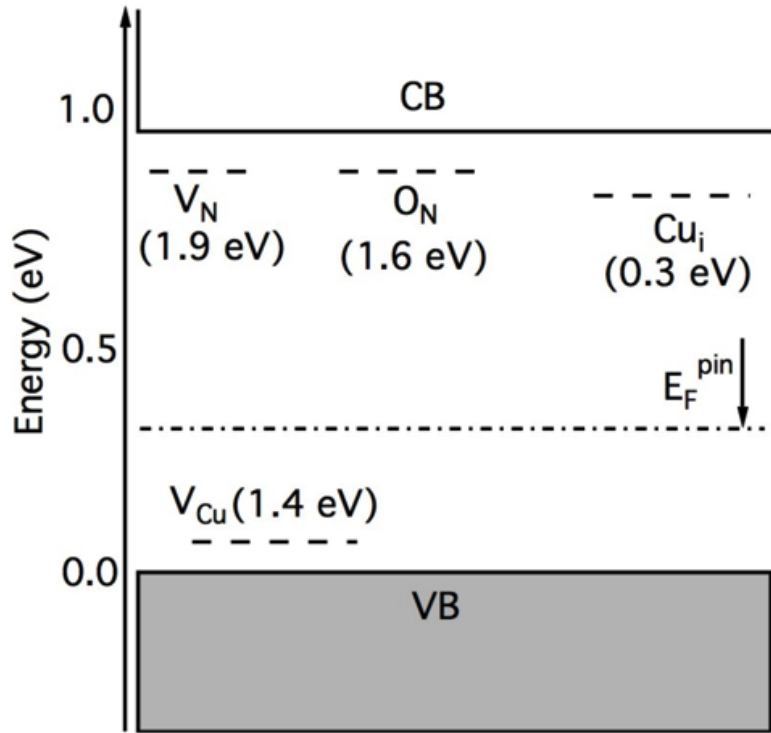


Sanity check: design principle at work



- Cu_3N surface show no surface states.
- GaN surface shows couple of surface states.

Formation energy of defects in Cu₃N



- No deep level in the gap
- p-type doping is achievable despite V_N and O_N
- Transition levels confirmed in conductivity measurements.

First case: CuTa₂N₂

Crystal structure: **delafossite**

■ **CuAlO₂: p-type TCO**

(Kawazoe *et al.*, Nature, 389,939 (1997))

■ **quasi-2D → large excitonic effect**

(Laskowski *et al.*, PRB, 79, 165209 (2009))

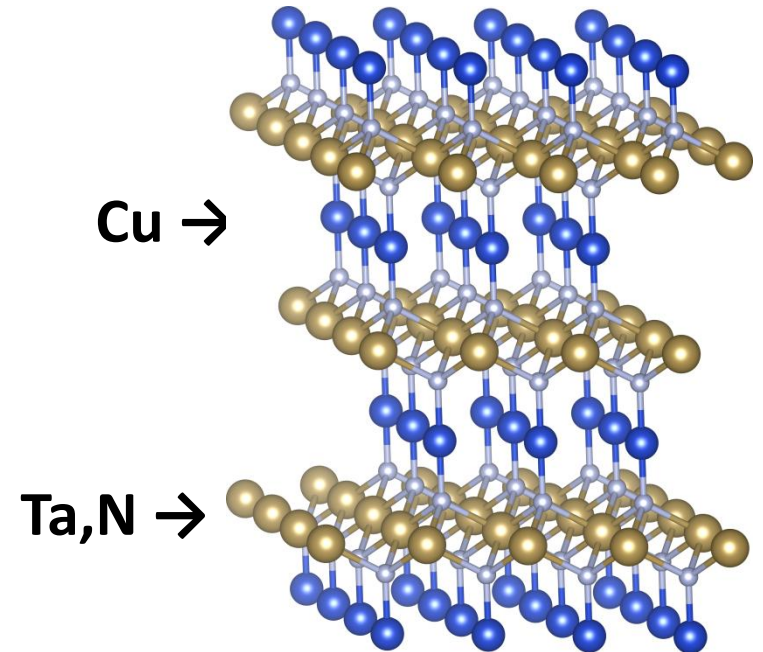
Synthesis: **ion exchange reaction**

■ **CuCl + NaTa₂N₂ → NaCl + CuTa₂N₂**

(Zachwieja, U.; Jacobs, H. *Eur J Sol State Inor* 1991, 28, 1055)

■ **CuI + NaTa₂N₂ → NaI + CuTa₂N₂**

(this work)

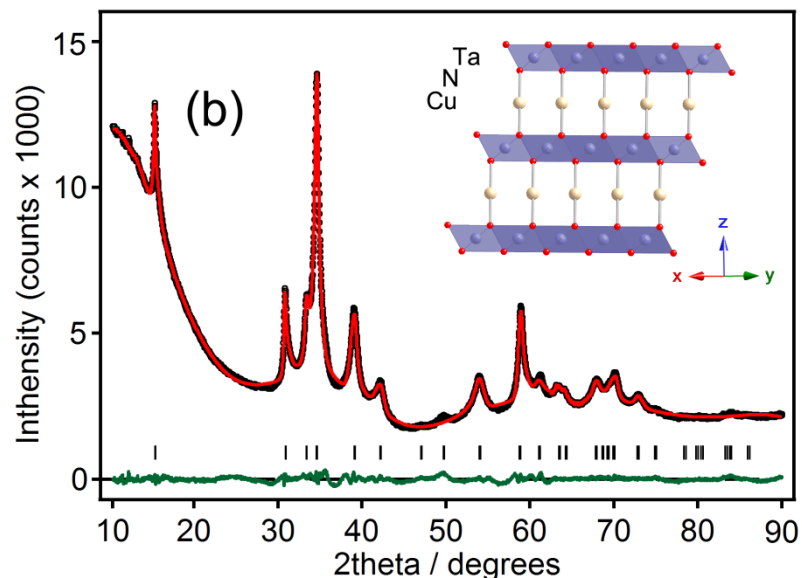
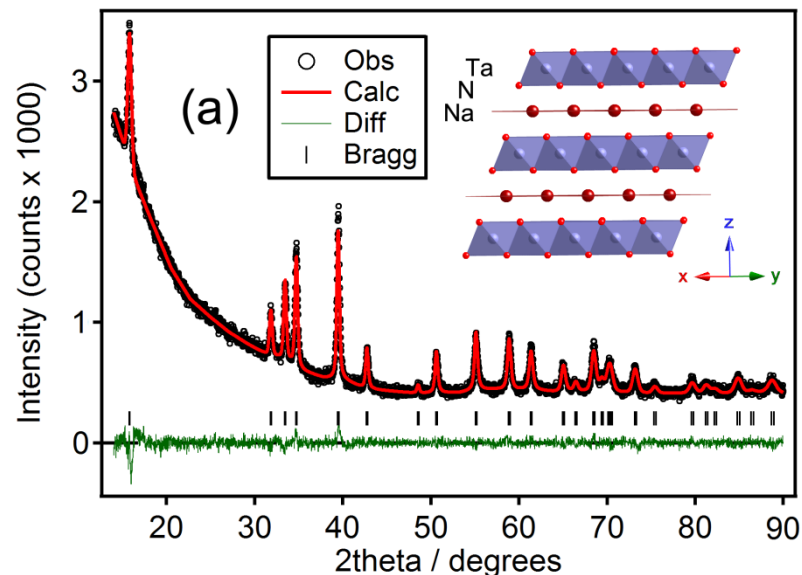
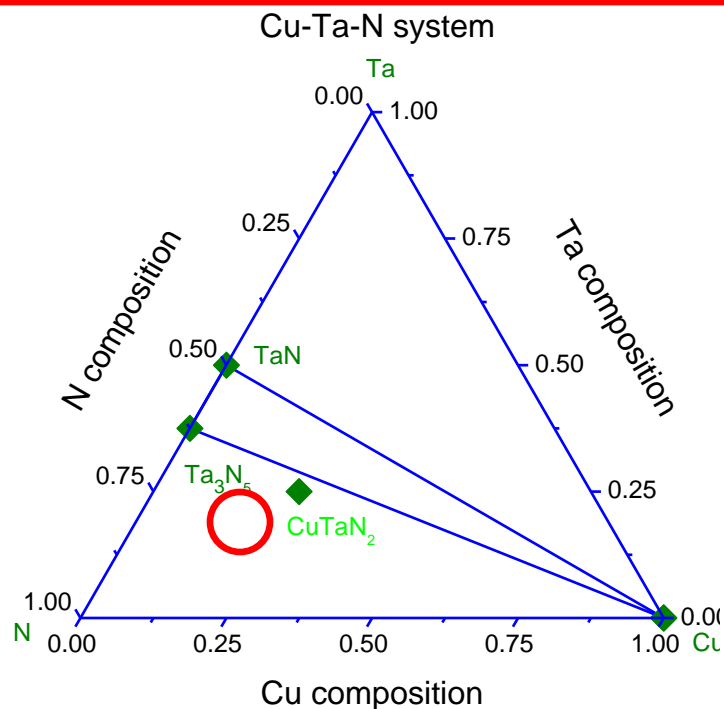


Yang M. *et al.*, accepted in Energy and Environmental Science, 2013

First case: CuTaN_2

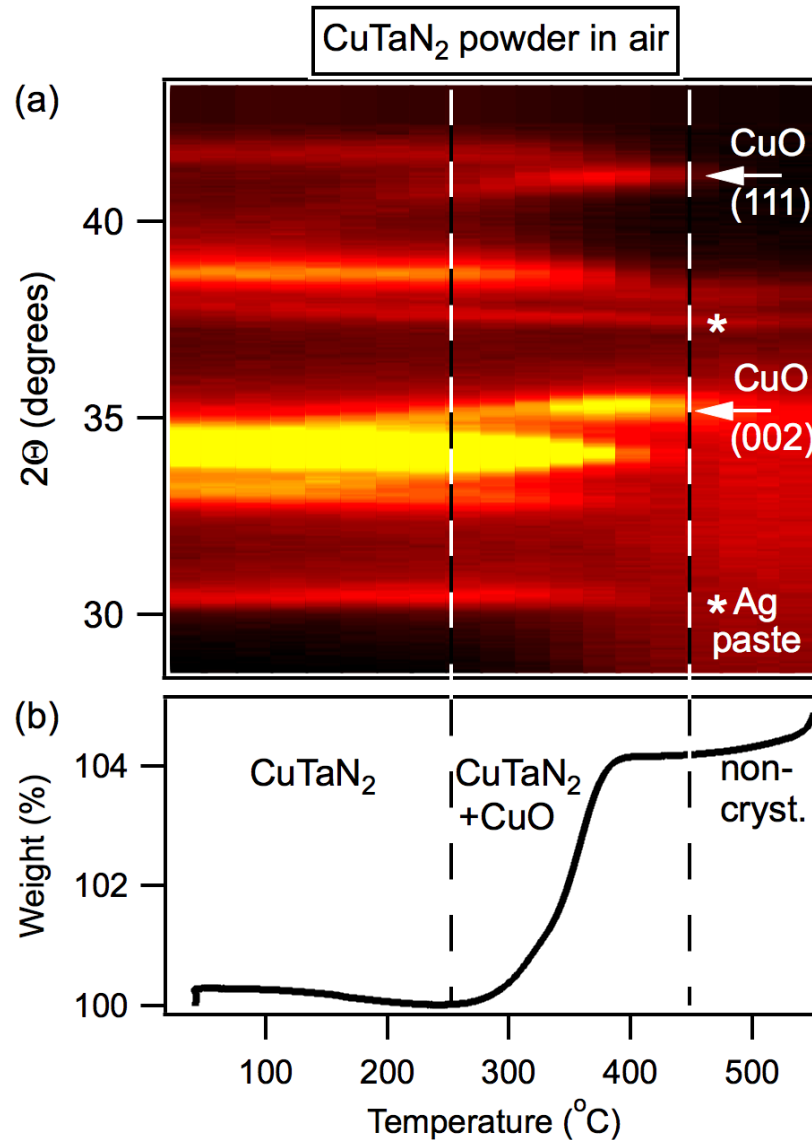
Results of synthesis

- **Different delafossite structure confirmed by theory.**
- **CuTaN_2 not thermodynamically stable wr to N_2 , Cu and Ta_3N_5**
- **Crystals with grains 50 to 300 nm**



Is CuTaN_2 PV-interesting ?

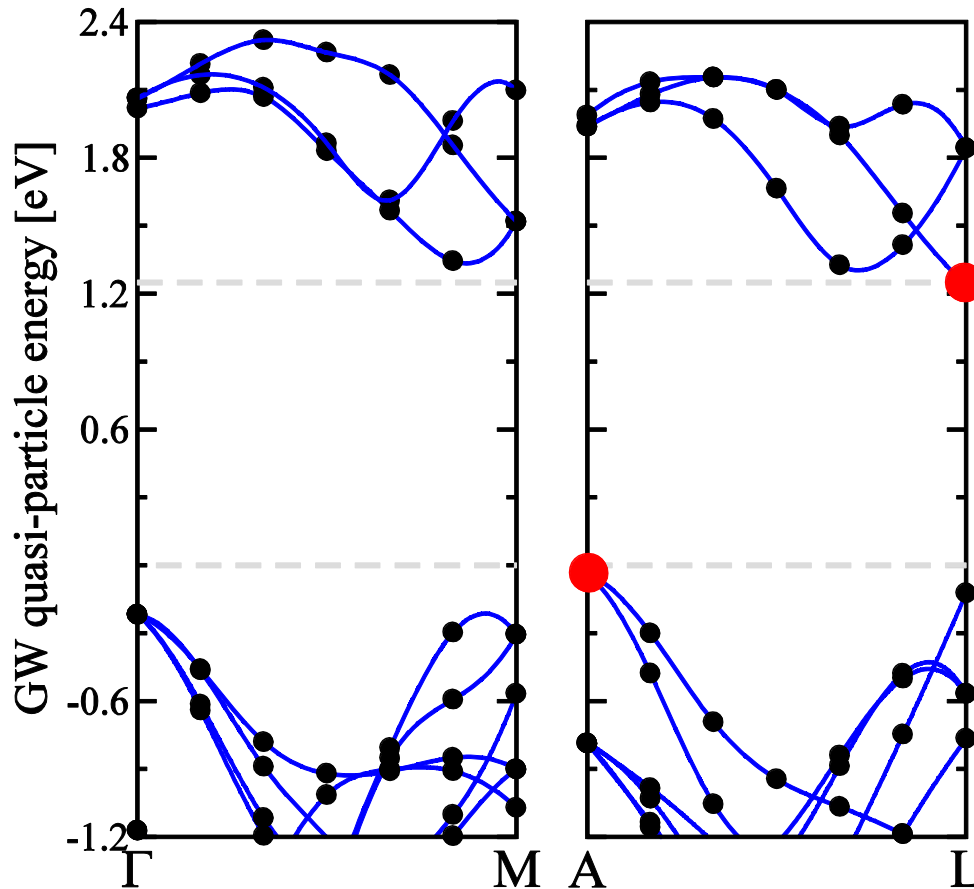
- Kinetic stability of CuTaN_2 : T-dependent XRD and TGA



Is CuTaN_2 PV-interesting ?

- Band structure and absorption properties

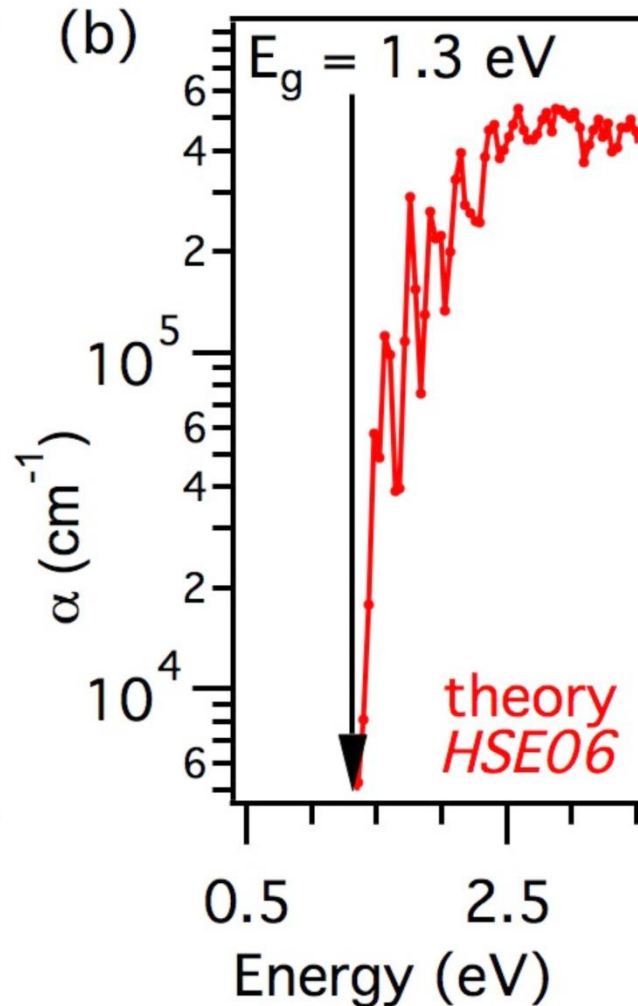
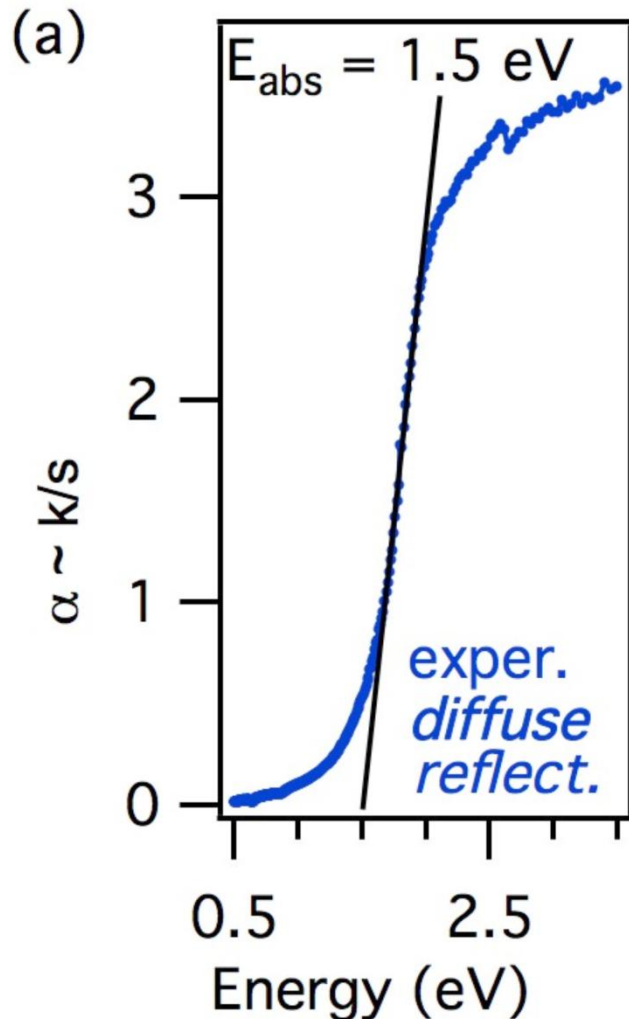
E_g is indirect at 1.3 eV with a direct transition at 1.5 eV



Is CuTaN₂ PV-interesting ?

- Band structure and absorption properties

High optical absorption at 1.5 eV !!!!

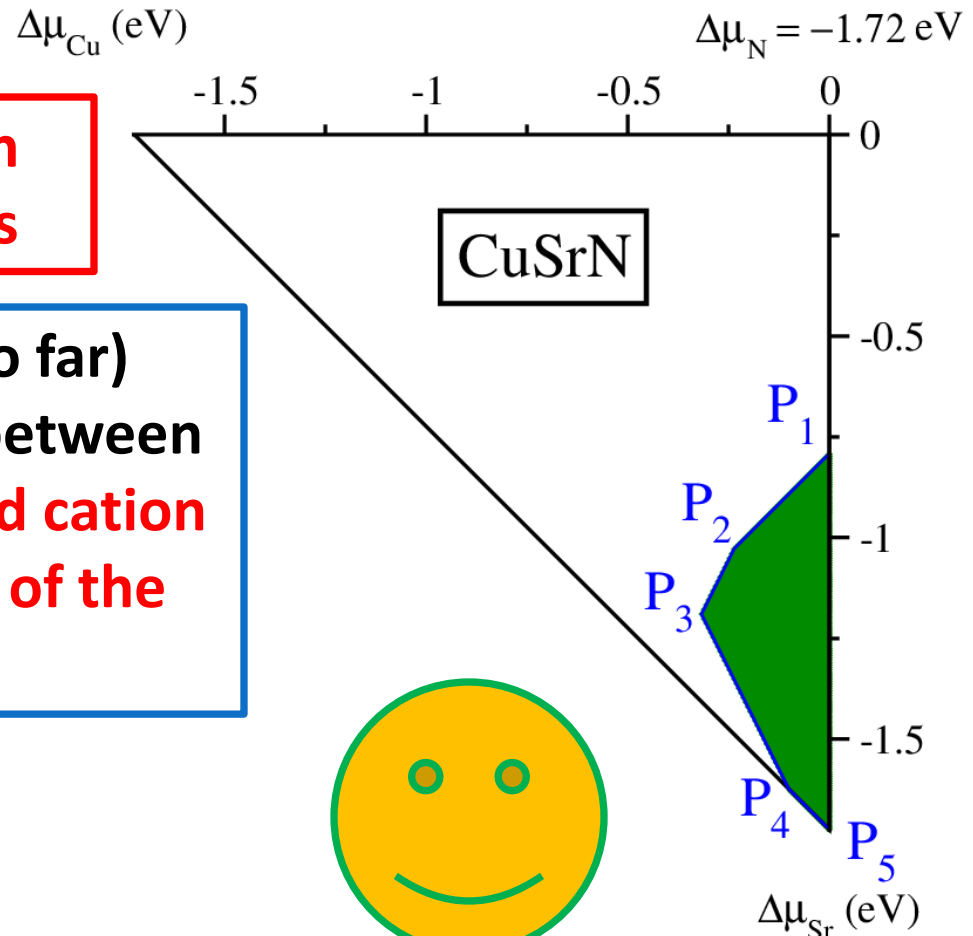


Second case: CuSrN

- Thermodynamically stable *i.e.* $\Delta H_f < 0$ and wr to binary and ternary compounds.

CuSrN stable under (N,Cu)-rich and Sr-poor growth conditions

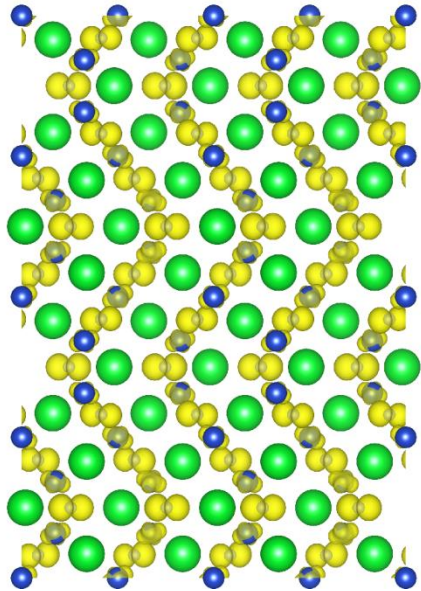
CuSrN only ternary stable (so far) because has to find a balance between attractivity of N with the second cation X and the formation enthalpy of the binary X_kN_l .



Is CuSrN PV-friendly ?

- A unique crystal structure → extraordinary conduction properties !!

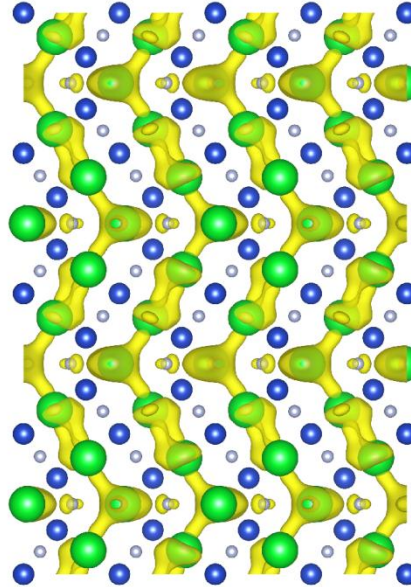
(a)



Valence band max

$$m_{\text{eff}}^x = 1.3 m_0$$

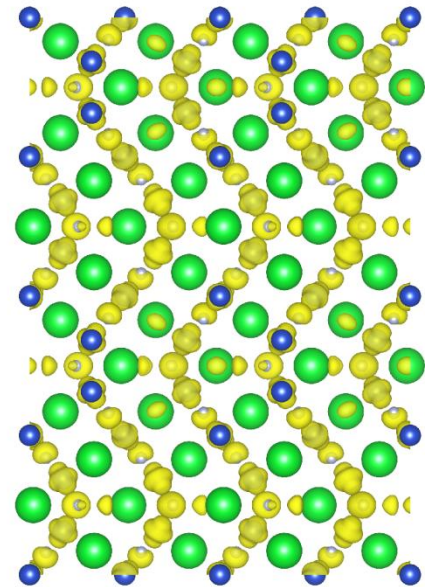
(b)



Conduction band min

$$m_{\text{eff}}^z = 0.05 m_0$$

(c)



Conduction band II

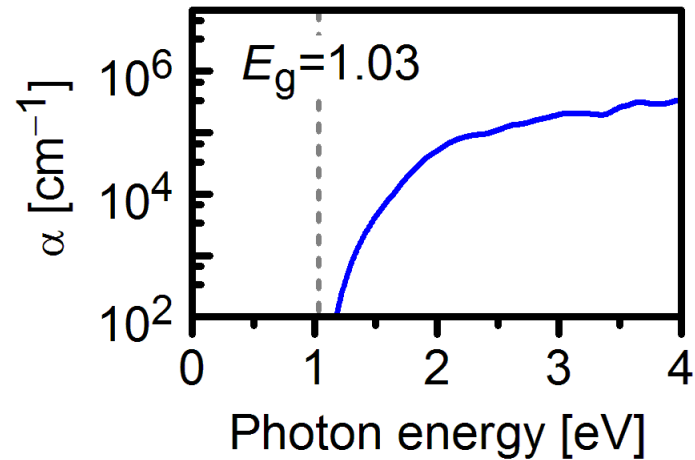
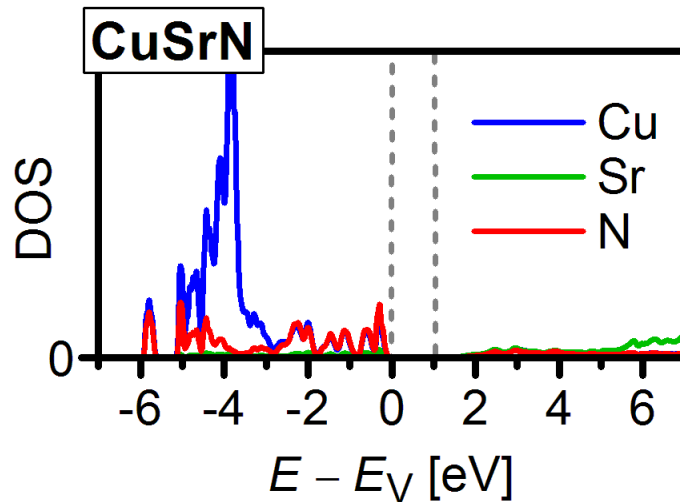
$$m_{\text{eff}}^z = 0.15 m_0$$



if p-type ...

Is CuSrN PV-friendly ?

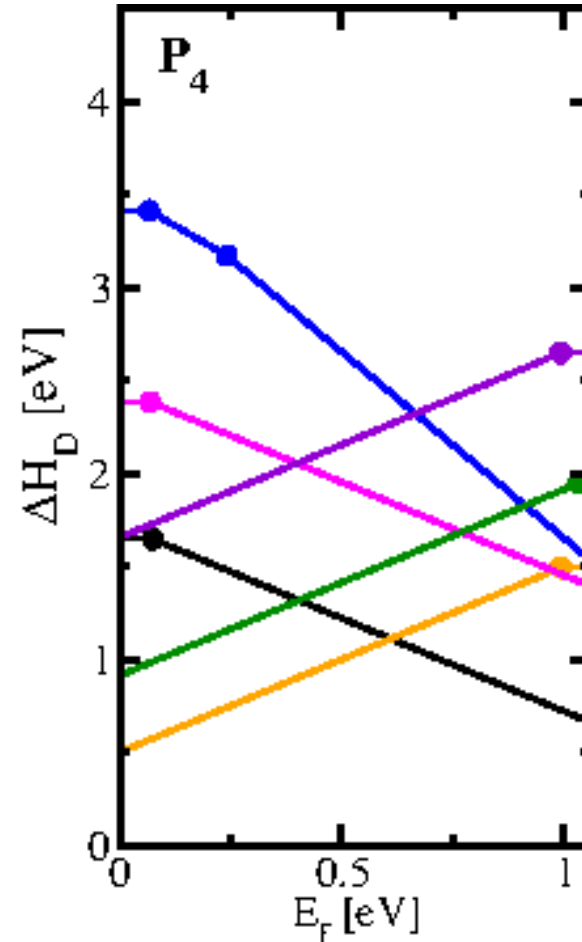
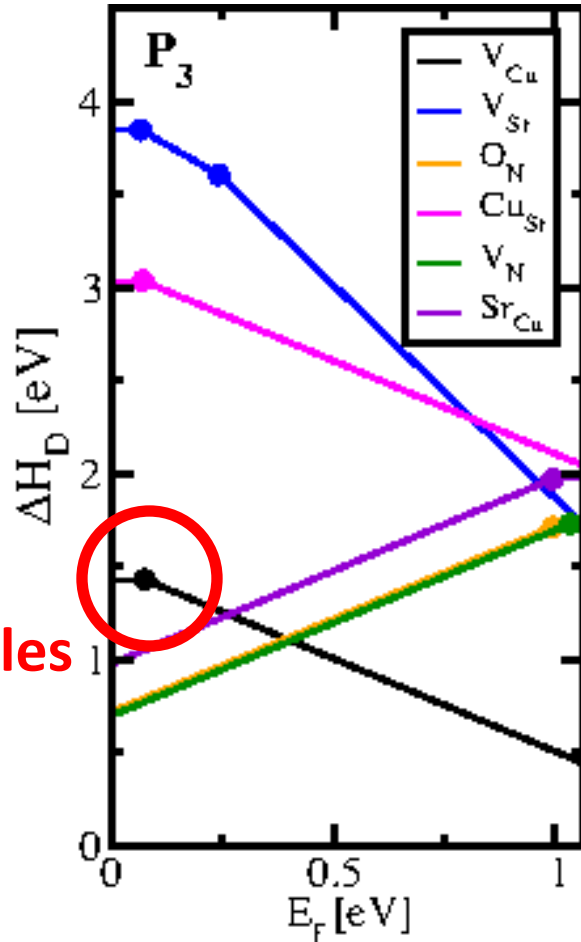
- Electronic properties: direct band gap ($E_g=1.03$ eV) with an optical transition at 1.3 eV !!!



Excitonic effect ? On-going work

Is CuSrN PV-friendly ?

- Ambipolar doping achievable ranging from moderate p-type



Origin of holes

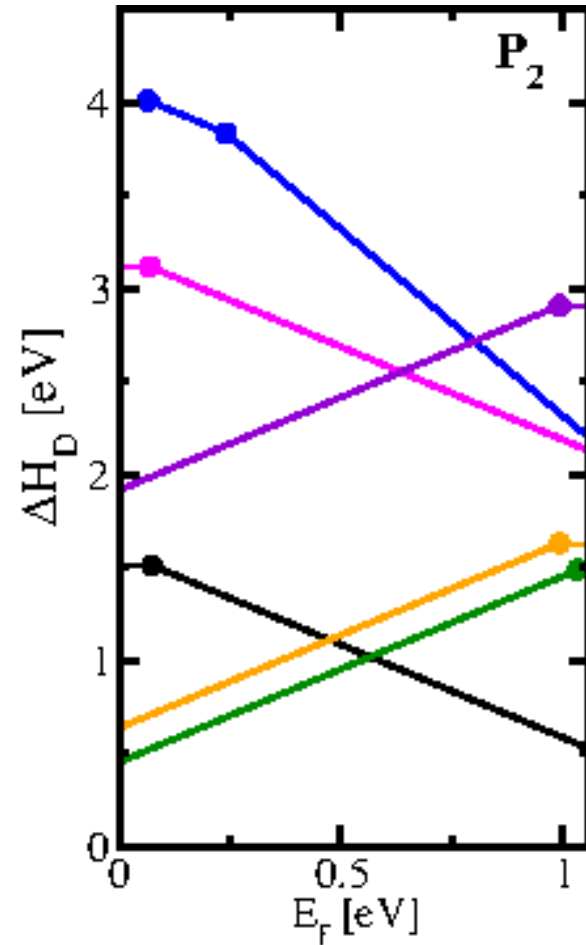
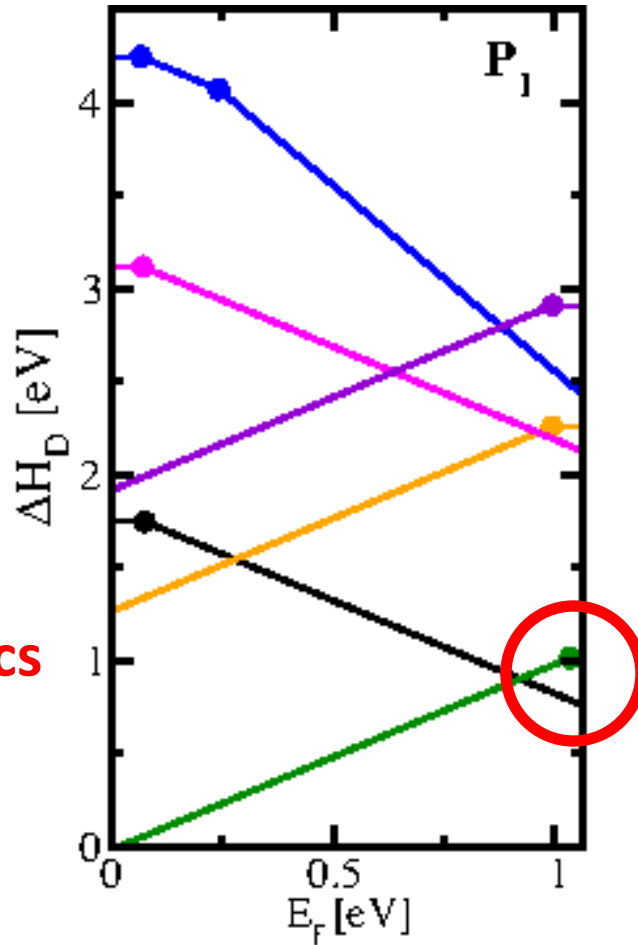
V_{Cu}

$$N_A = 3-6 \times 10^{16} \text{ cm}^{-3}$$



Is CuSrN PV-friendly ?

- to highly doped n-type: HOMOJUNCTION !!!



Origin of elects

V_N

$$N_D = 6 \times 10^{19} \text{ cm}^{-3}$$





4

PROJECT SNS

SnS: an « old » PV material

•What makes SnS attractive?

- ✓ Earth abundant inexpensive elements
- ✓ Band gap near optimal (often quoted as 1.3 eV direct gap)
- ✓ Synthesis methods:
Solution-based, physical vapor, chemical vapor
- ✓ “Buffer layer” issue:
 - ✓ Homojunction: ambipolar dopability (G. Yue *et al.*, J. Mater. Chem. **22**, 16437, 2012)
 - ✓ Tunable window layer (Sinsermsuksakul *et al.*, APL, **102**, 053901, 2013)

APPLIED PHYSICS LETTERS **100**, 032104 (2012)

Band-structure, optical properties, and defect physics of the photovoltaic semiconductor SnS

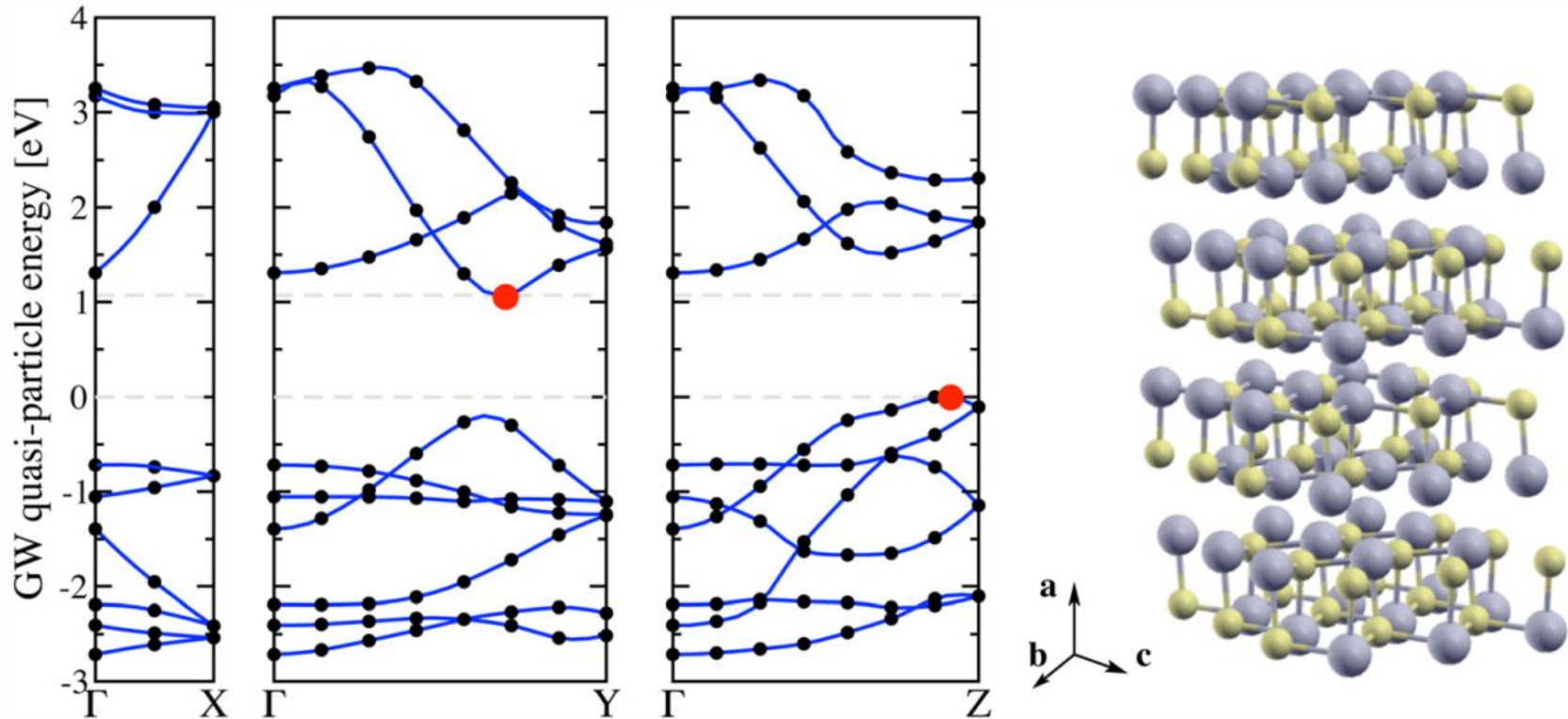
Julien Vidal,¹ Stephan Lany,^{1,a)} Mayeul d’Avezac,¹ Alex Zunger,^{1,b)} Andriy Zakutayev,^{2,c)}
Jason Francis,² and Janet Tate²

¹National Renewable Energy Laboratory, Golden, Colorado 80401, USA

²Department of Physics, Oregon State University, Corvallis, Oregon 97331, USA



Band structure of SnS



- Band gap of 1.07 eV is **indirect**

- Effective masses:

Minority carriers (electrons): $m_{\perp}^* = 0.5 m_e$, $m_{\parallel}^* = 0.2 m_e$

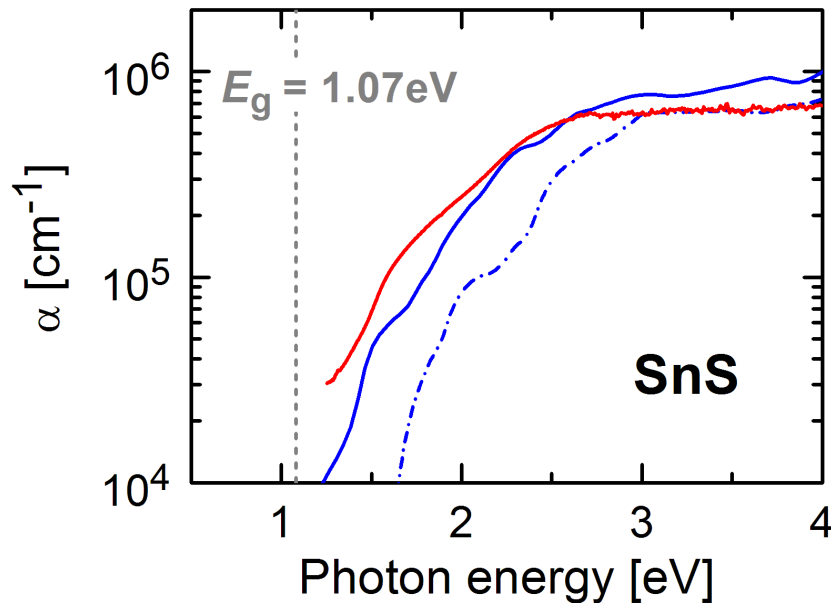
Majority carriers (holes): $m_{\perp}^* = 1.5 m_e$, $m_{\parallel}^* = 0.3 m_e$

- ALD-grown SnS oriented either \perp or \parallel to substrate (P. Sinsermsuksakul *et al.*, Adv. En. Mat., 1, 1116 (2011)) \rightarrow Different collection length when buffer tuned ?

Optical absorption: theory and experiments

Band gap (E_g) vs absorption threshold (E_{abs})

- E_g determines max. V_{OC} ($V_{OC} - E_g = 0.3$ eV (GaAs) to 0.6 eV (CdTe))
- E_{abs} determines photon collection (J_{SC})



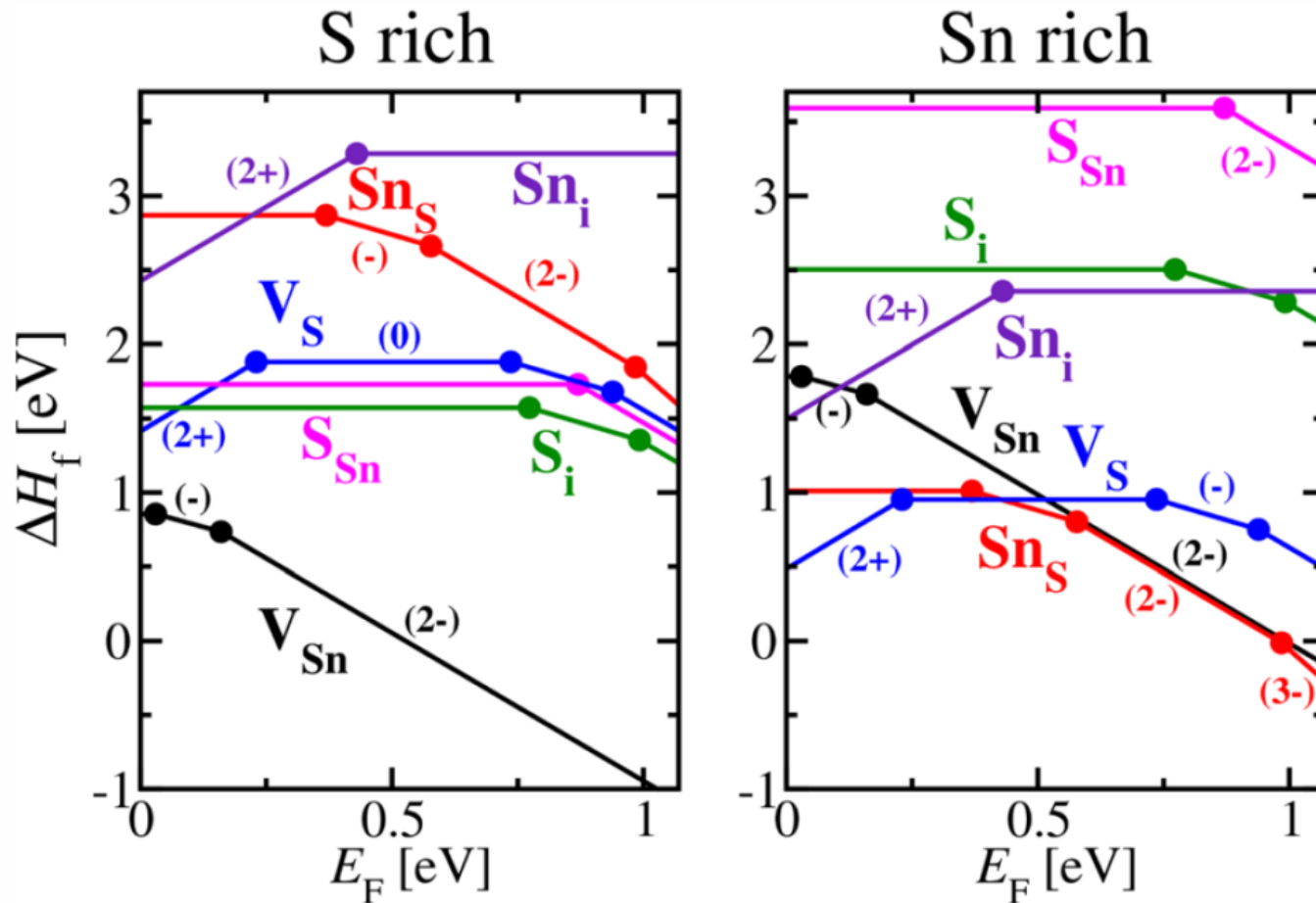
Measured and calculated optical absorption spectra

- Experiment
- - - GW (independent particle)
- GW (+ excitonic effects)

Theory includes direct-allowed transitions, but no phonon-assisted or disorder-induced indirect or forbidden transitions

- Effective absorption threshold: $E_{abs} \sim 1.5$ eV lies ~ 0.4 eV above E_g
- Small V_{OC} obtained in practice 0.3 eV despite new buffer (except for SnS NW)

Defect formation energy



- Sn-vacancies (V_{Sn}) are native p -type dopant
- Deep defects (V_S , Sn_S) acting as recombination centers form under S-rich conditions

From defect formation energy to carrier concentration

Defect formation energy

$$\Delta H = \Delta H_{D,q}(\mu, E_F)$$

Defect concentration

$$c_D \approx N_{\text{site}} \times \exp(-\Delta H/kT)$$

Electron/hole density

$$c_e = \int f_{\text{FD}}(E - E_F) g(E) dE$$

Charge neutrality

$$-c_e + c_h + \sum [q \cdot c(D^q)] = 0$$

Self-consistent solution

$$\Delta H(E_F) \quad c_D(\Delta H) \quad E_F$$

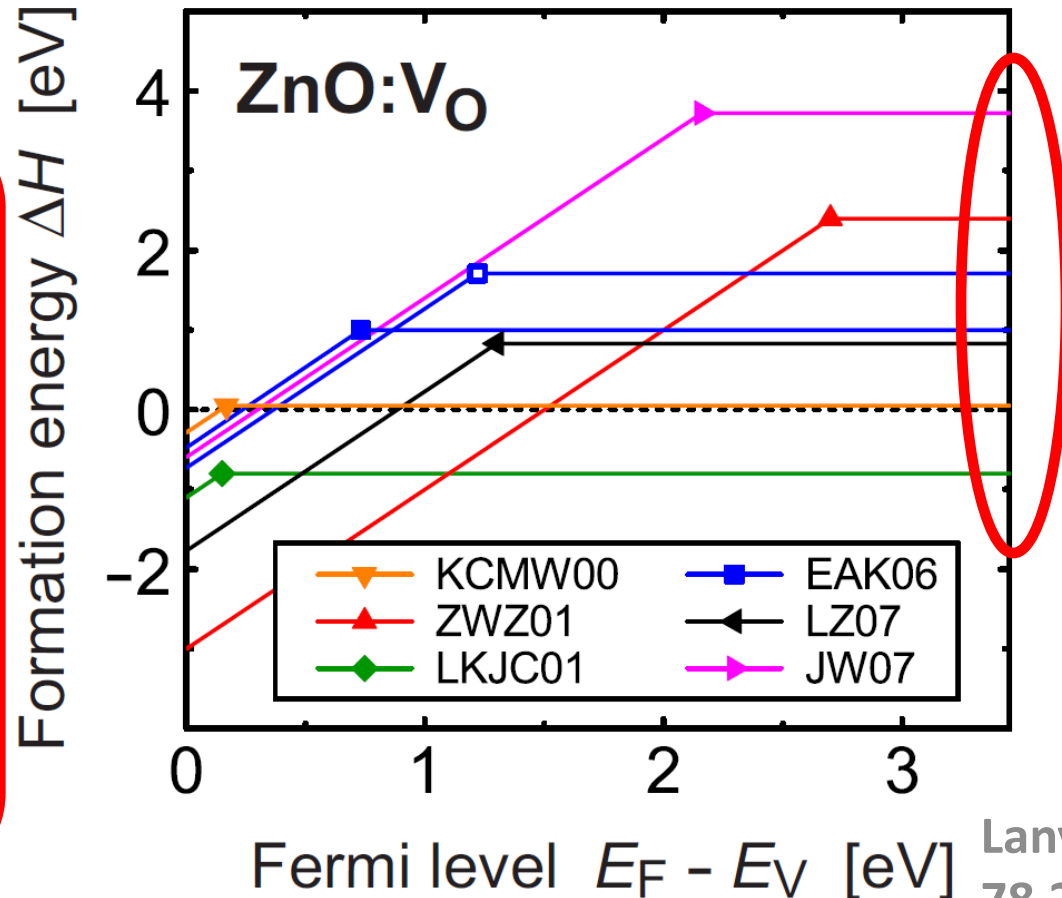
pO_2 dependence of μ_o
(ideal gas)

$$\begin{aligned} \Delta\mu_o(T, P_0) &= \frac{1}{2} [H_0 + \Delta H(T)] - \frac{1}{2} T \cdot [S_0 + \Delta S(T)] \\ \Delta\mu_o(T, P) &= \Delta\mu_o(T, P_0) + \frac{1}{2} kT \ln(P/P_0) \end{aligned}$$

- High conc. Account for competition of defects and host atoms for N_{site}
Association/dissociation of *defect-clusters* (law of mass action)
- Direct Given $\Delta H(\mu)$, find concentrations c_D
- Inverse Given a target concentration, find ΔH (i.e., find μ)

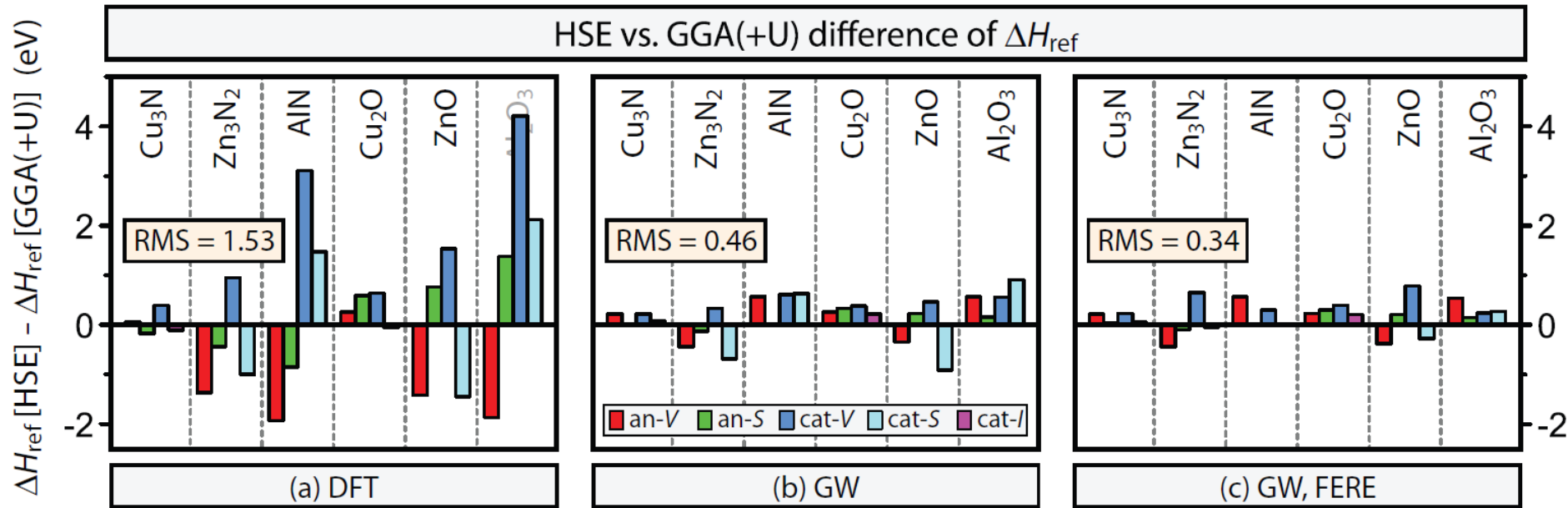
Are defect formation energy good enough ?

Difference in transition levels is linked to the gap underestimation by DFT. Therefore, **people use hybrid functional for total energy because it gives the right band gap.**



Transition levels were the main concern but absolute formation energies display large variations too !!!

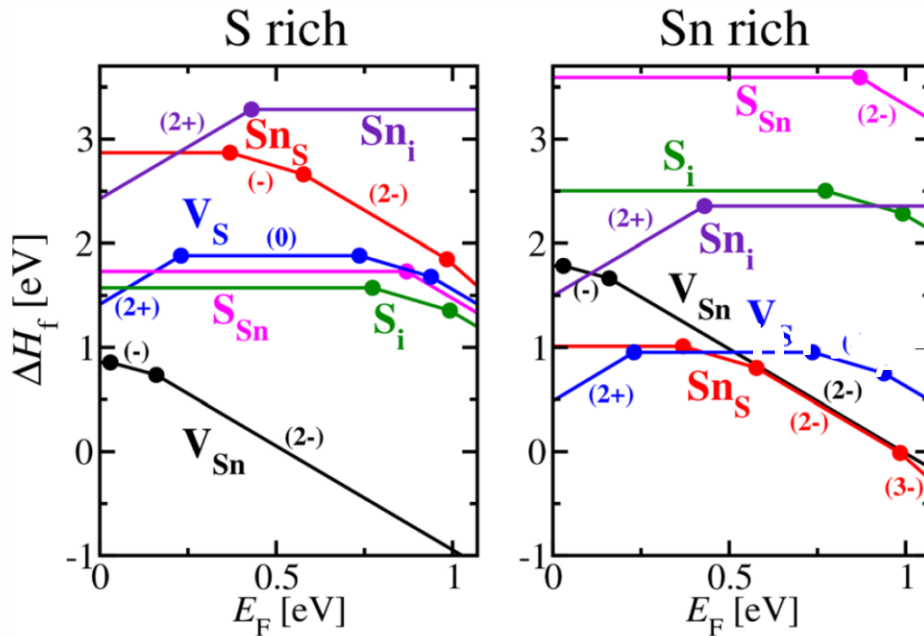
Unification of hybrid and DFT formation energy



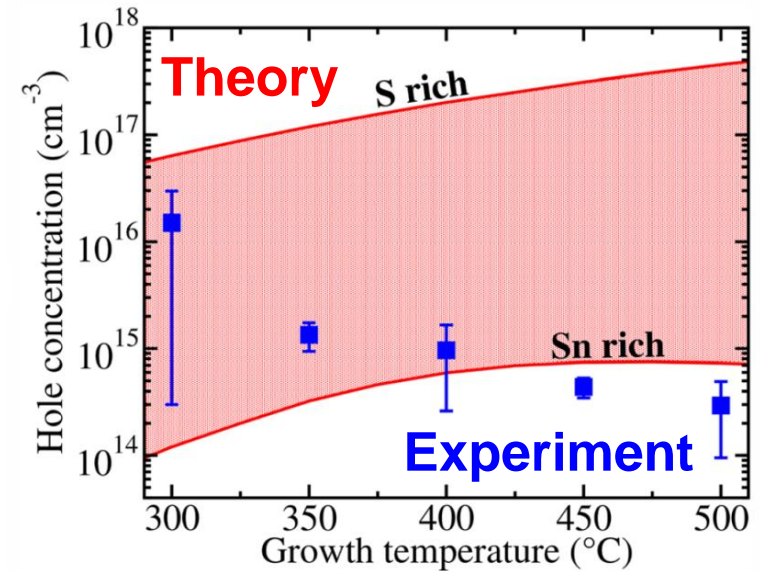
- Compounds heat of formation should be corrected by a fitting mechanism FERE
- For **shallow defects**, GW corrections must be added
- Sanity check: GW corrections must give the right ionization energy.
- Conclusion: **HSE06 and DFT can be made equivalent**

Carrier concentration and PV assessment

DFT supercell calculations for defects in SnS



Thermodynamic modeling of doping and Hall-measurements



- $p = 10^{14}-10^{17}$ cm^{-3} due to V_{Sn}
- Sulfur-rich growth is desired to avoid deep centers (V_S , Sn_S): Reduced V_{oc}
- Trade-off with growth temperature



5

PROJECT CZTS

$\text{Cu}_2\text{ZnSnS}_4$ (CZTS)

- Based on the compound CuInS_2 , replace 2 In by 1 Sn and 1 Zn.
- Historically, CZTS was thought to be the same as CIGS.

BUT

- Phase diagram is much more complex due to binary and ternary compounds.
- ZnS is very stable and always present in thin films.
- SnS tends to evaporate and forms detrimental voids.
- Efficiency of devices has been limited to **11%** under **wet process** while the best CIGS-based devices are made in **vacuum**.

How to compute a phase diagram ?

- **Competing binary and ternary compounds**

- ✓ **Cu-Sn-S:** Cu_2SnS_3 , Cu_4SnS_4 , Cu_4SnS_6 , $\text{Cu}_4\text{Sn}_7\text{S}_{16}$
- ✓ **Cu-S:** Cu_2S , Cu_9S_5 , Cu_7S_4 , CuS , CuS_2
- ✓ **Sn-S:** SnS , SnS_2 , Sn_2S_3
- ✓ **ZnS**

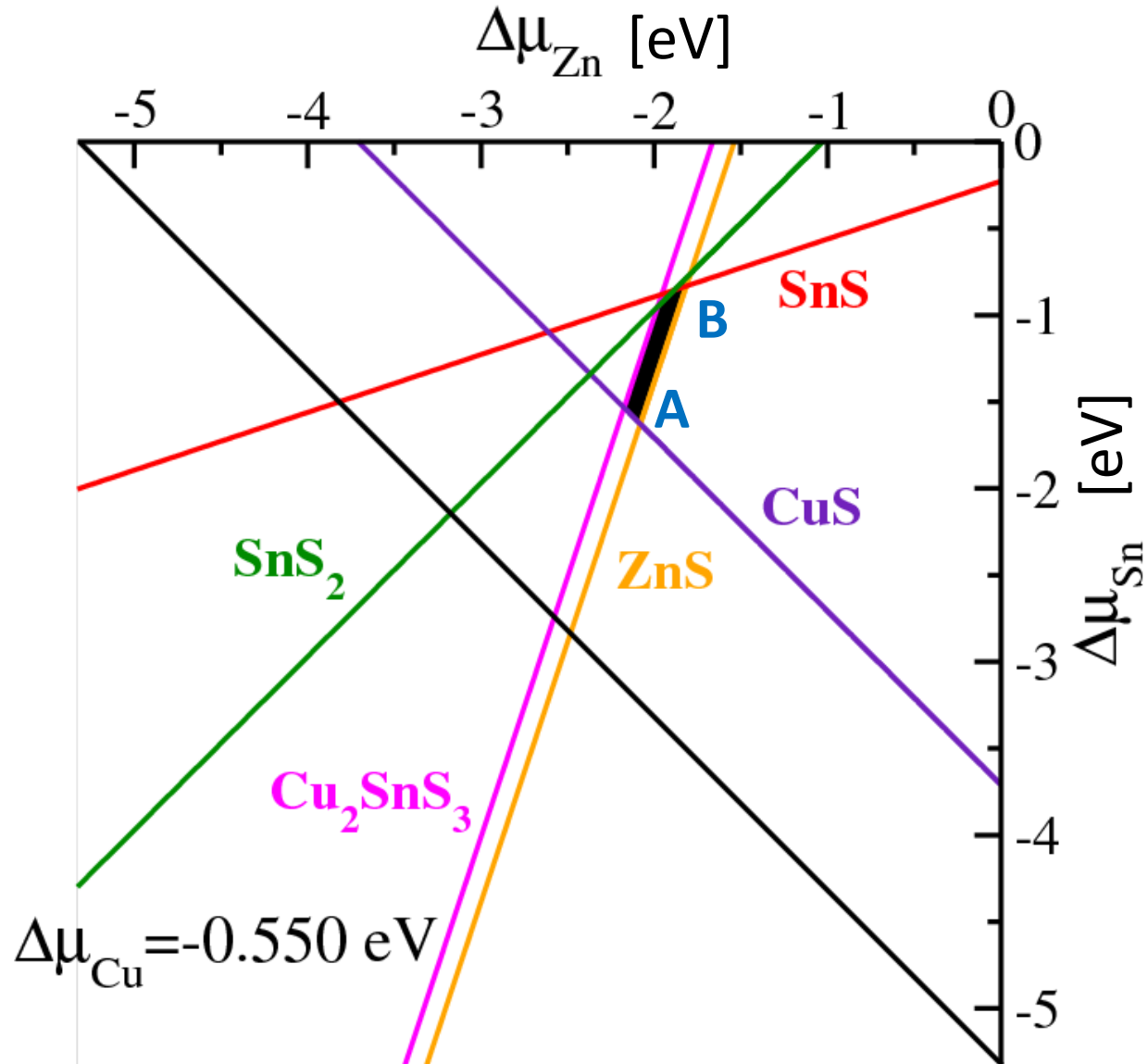
- **Ab initio-calculated phase diagram**

- ✓ Define the deviation of the chemical potential w.r.t. standard ref.
- ✓ Preventing formation of competing phases with condition
- ✓ Allowing formation of CZTS

$$a\Delta\mu_A + b\Delta\mu_B + c\Delta\mu_X < \Delta H_f(A_a B_b X_c)$$

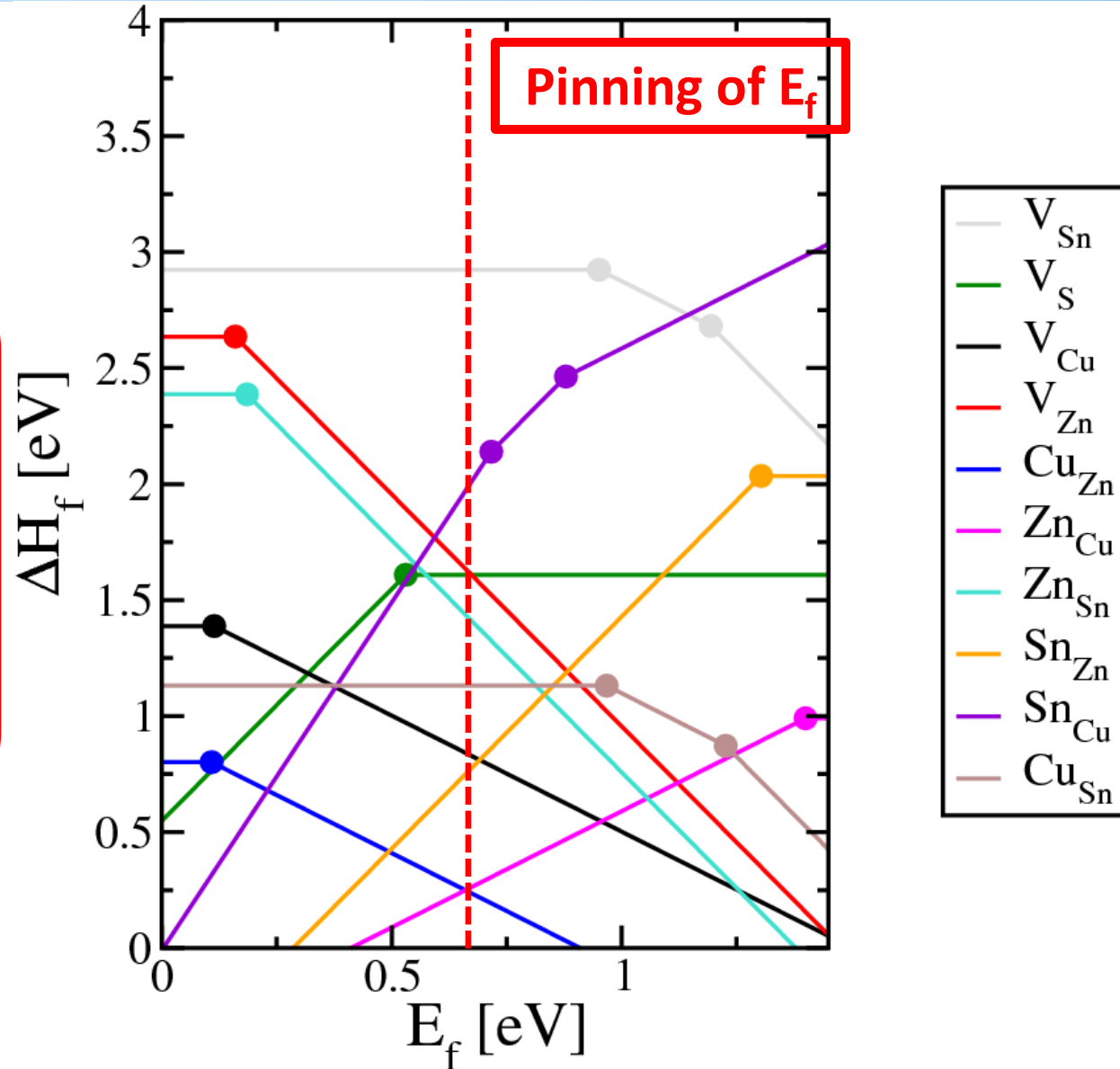
$$2\Delta\mu_{\text{Cu}} + \Delta\mu_{\text{Zn}} + \Delta\mu_{\text{Sn}} + 4\Delta\mu_{\text{S}} = \Delta H_f(\text{CZTS})$$

Phase diagram of CZTS

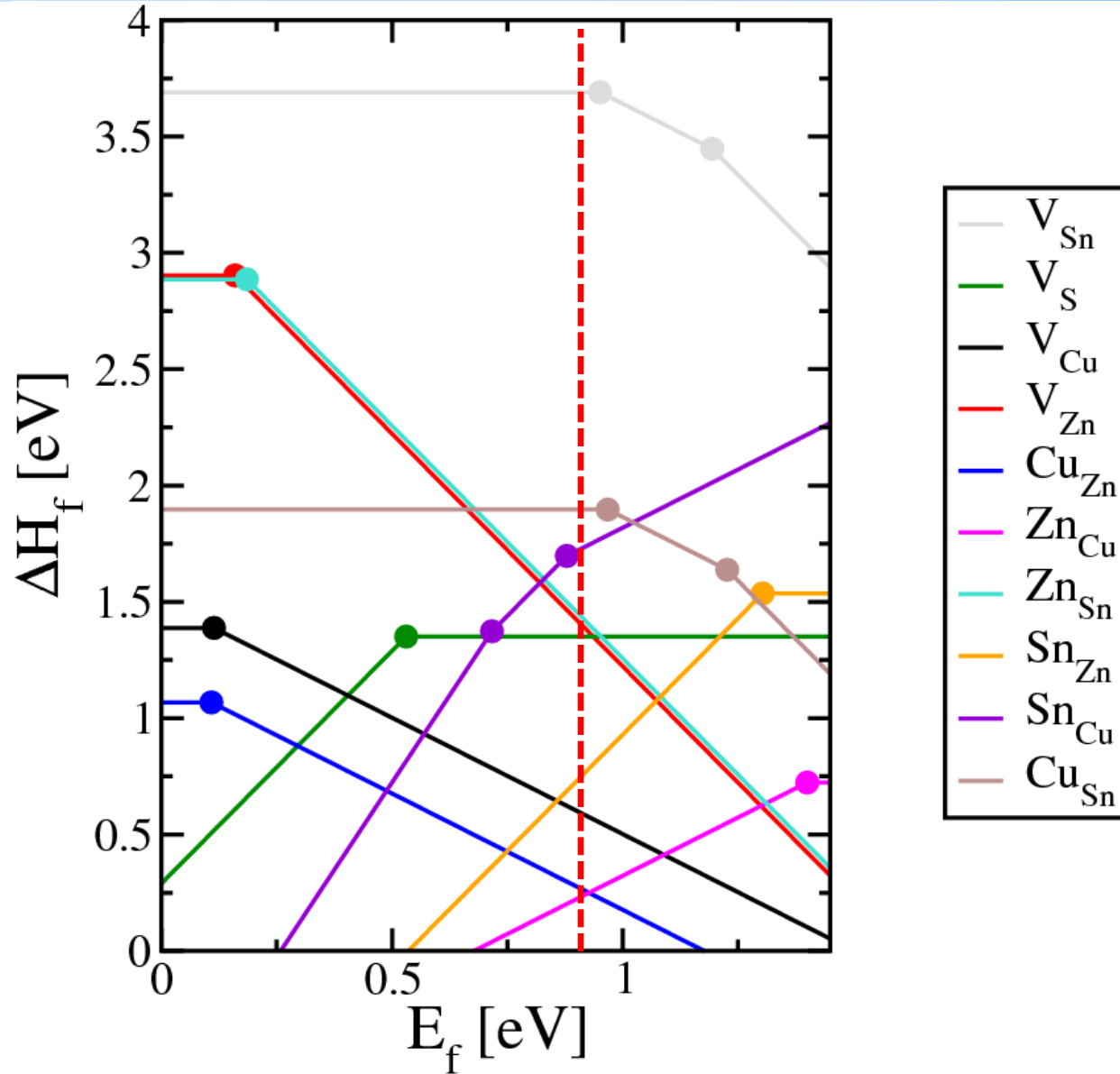


Defect formation energy at A

- Copper vacancy is not the main defect as in CIGS.
- Cu_{Zn} and Zn_{Cu} have similar formation energy.
- CZTS is highly **compensated** materials, with **intrinsic conductivity** limiting efficiency.



Defect formation energy at B





3

CONCLUSIONS AND PERSPECTIVES

Conclusions and perspectives

- Search for new materials allow to understand better existing champion materials.
- Technological applications and material properties are narrowly linked.
- PV is not about light absorption, famous counterexample being Si.
- Apparent harmless change of a material can have deep consequences like CZTS.
- Explore the unexplored without any industrial or economical constraints because it can shine light on the existing phenomenon